

Spring 2010 MA521 Classical Complex Analysis

last updated: Feb 22nd (Monday)

Course Name: Classical Complex Analysis

Class Time/Location: MWF 11:00~11:50 at Science Center 340

Office: Science Center 385

Office Hours: MWF 9:15~11:00 or by appointment (just send me an email in advance).

Instructors:

Jie Sun (Weeks 1~8)

[course webpage: www.sunjie1984.com/MA521/MA521Syllabus.pdf]

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Ye Chen (Weeks 9~16)

Textbook:

[Complex Analysis, 4th edition](#), by *Serge Lang*.

Prerequisites: MA 321 or equivalent.

Main Topics: Complex number system, Cauchy-Riemann Equations, Analyticity and Power Series, Cauchy's Theorem, Winding Numbers, Cauchy's Integral Equation, Calculus of Residues, Conformal Mappings, The Riemann Mapping Theorem.

Homework: Assigned after each section and will be collected *every Monday in class*.

Exams: Closed book.

Grading Scheme:

Homework:	60%	
Midterm Exam:	20%	Feb. 24th (Wed) 7pm
Final Exam:	20%	(TBA)

Letter grades for course are assigned as follows:

90~100:A, 85~89:B+, 80~84:B, 75~79:C+, 70~74:C, 65~69:D+, 60~64:D, <60:F.

Course Learning Objectives:

Student are expected to acquire graduate level/professional mathematical skills such as presenting rigorous proofs, and gain a solid understanding of classical complex analysis. Those will be achieved through hard/efficient work by both us (instructors) and you (the students).

Schedule:

Date	#	Section	Contents	Assignments
Jan. 8 (Fri)	L0	1.1	Definition of Complex Numbers	HW1(A): Ex. 1.1 (p. 7) #1(a~d), #3, #6, #8, #10(a,e).
Jan. 11 (Mon)	L1	1.2,1.3	Polar Form Representation, Complex Valued Functions	HW1(B): Ex. 1.2 (p. 11) #1(a~d), #2(a~d), #6, #11, #12. Ex. 1.3 (p. 17) #1, #2, #3.
Jan. 13 (Wed)	L2	1.4	Limits and Compact Sets	HW1(C): Ex. 1.4 (p. 26) #1, #4, #6, #7.
Jan. 15 (Fri)	L3	1.4,1.5, 1.6	Compact Sets (cont.), Complex Differentiability, & Cauchy-Riemann Eqs	HW1 Due: Jan. 18 (Mon).
Jan. 18 (Mon)	L4	1.6, 1.7	Cauchy-Riemann Eqs proof. (cont.)	In class presentation on Cauchy-Riemann Eqs. in polar form. <i>Bonus: Andrew Davis</i>
Jan. 20 (Wed)	L5	1.6, 2.1	Angles under Holomorphic Maps & Formal Power Series	HW2(A): Ex. 2.1 (p. 46) #1(a,c,f), #3, #4. <i>[Hint of #3: multiply both sides by (e^z-1) and expand in power series.]</i>
Jan. 22 (Fri)	L6	2.2	Convergent Power Series	HW2(B): Ex. 2.2 (p. 58) #3, #4, #5, #7, #9(*), #10, #11. (This is a lot...) HW2 Due: Jan. 27(Wed)
Jan. 25 (Mon)	L7	2.3, 2.4	Formal vs Convergent Power Series & Analytic Functions	None!

Date	#	Section	Contents	Assignments
Jan. 27 (Wed)	L8	2.4, 2.5	Analytic Functions & Differentiation of Power Series	HW3(A): Ex. 2.3 (p. 68) #2, #5. [Hint: #2(a) apply Theorem 3.2(p.62) on uniqueness.] HW3(B): Ex. 2.4 (p. 71) #1, #2 HW3(C): Ex. 2.5 (p. 75) #2, #3, #6.
Jan. 29 (Fri)	L9	2.6, 2.7	Inverse and Open Mapping Theorems & Local Maximum Modulus Principle	HW3(D): Ex. 2.6 (p. 83) #1, #2, #3, #4, #5. Due: Feb. 1(Mon)
Feb. 1 (Mon)	L10	3.1	Connectedness and Holomorphic Functions on Connected Sets	HW4(A): Ex. 3.1 (p. 93) #1, #2, #3.
Feb. 3 (Wed)	L11	3.2	Integrals over Paths	HW4(B): Ex. 3.2 (p.102) #1, #2, #5, #7, #9, #10.
Feb. 5 (Fri)	L12	3.3	Local Primitive for a Holomorphic Function	HW4(C): Ex. 3.2 (p.102) #11. [To be presented in next Monday's class, by ?] Due: Feb. 10(Wed)
Feb. 8 (Mon)	L13	3.4	Another Description of the Integral Along a Path	<i>Ex. 3.2 #11 presented by Sean Kramer in class.</i>
Feb. 10 (Wed)	L14	3.5	The Homotopy Form of Cauchy's Theorem	HW5: Ex. 3.4 (p.118) #1, #2, #3, #4. Due: Feb. 15(Mon)
Feb. 12 (Fri)	(no)			Pick your favorite special function and study it.
Feb. 15 (Mon)	L15	3.6	Existence of Global Primitives. Definition of the Logarithm	<i>Polylogarithm function presented by Dillon Ethier.</i>

Date	#	Section	Contents	Assignments
Feb. 17 (Wed)	L16	3.7	The Local Cauchy Formula	HW6: Ex. 3.6 (p.125) #1(c,f,g,h), #2(c,d,e,h), #3, #4, #6(*), #7, #8. (*): bonus problem. HW6: Ex. 3.7 (p.132) #1, #2, #3. Due: Feb. 22(Mon)
Feb. 19 (Fri)	L17		Review of Mid-term Exam	
Feb. 22 (Mon)	L18	4.1	The Winding Number	HW7: Ex. 4.2 (p.149) #1, #2, #3. Due: March. 1(Mon)
Feb. 24 (Wed)	L19	4.2	The Global Cauchy Theorem	
Feb. 26 (Fri)	L20	4.2	(cont.) The Global Cauchy Theorem	